

Unit 13

Day 5

Inverse Functions - continued

Let f be a one-to-one function. Then g is the inverse function of f if

$$(f \circ g)(x) = x \quad \text{for every } x \text{ in the domain of } g .$$

$$(g \circ f)(x) = x \quad \text{for every } x \text{ in the domain of } f .$$

Determine if the functions are inverses.

1) $f(x) = x^3 - 2$ $g(x) = \sqrt[3]{x+2}$

$$f \circ g = f(g(x)) = f(\sqrt[3]{x+2}) = (\sqrt[3]{x+2})^3 - 2 = x+2-2 = x \checkmark$$
$$g \circ f = \sqrt[3]{(x^3-2)+2} = \sqrt[3]{x^3} = x \checkmark$$

$$f(x) = x^3 - 2$$

$$x = y^3 - 2$$

$$\sqrt[3]{x+2} = y$$

$$\sqrt[3]{x+2} = y$$

$$g(x) = \sqrt[3]{x+2}$$

$$x = \sqrt[3]{y+2}$$

$$x^3 = y+2$$

$$x^3 - 2 = y$$

yes, they are
inverse

Determine if the functions are inverses.

2) $f(x) = \sqrt{\frac{1}{3}x + \frac{4}{3}}$ $g(x) = 3x^2 - 4$

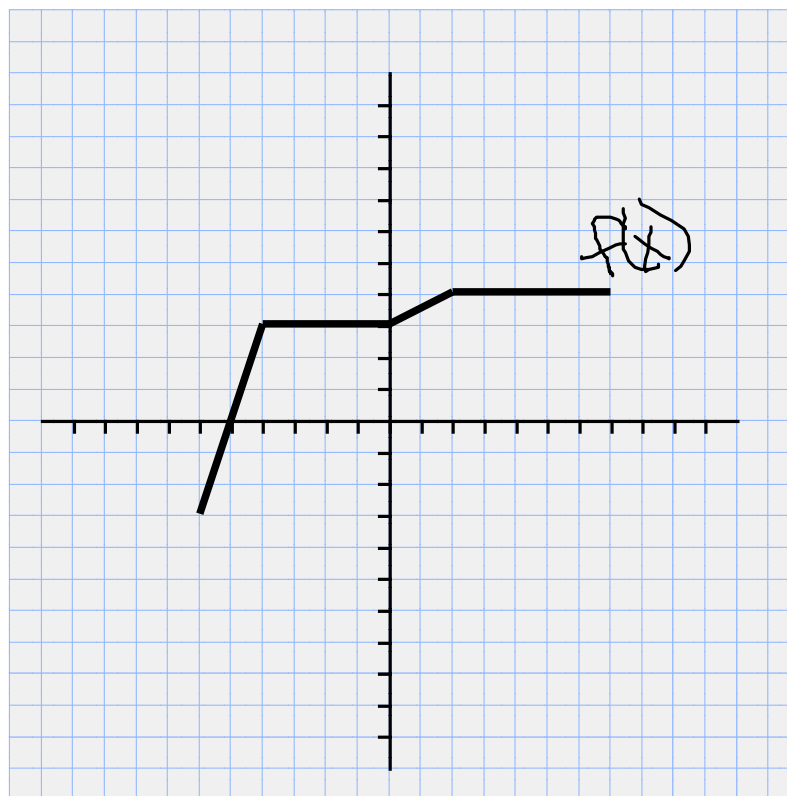
$$\begin{aligned} f \circ g &= \sqrt{\frac{1}{3}(3x^2 - 4) + \frac{4}{3}} \\ &= \sqrt{x^2 - \frac{4}{3} + \frac{4}{3}} \\ &= \sqrt{x^2} \\ &= x \quad \checkmark \end{aligned}$$

$$\begin{aligned} g \circ f &= 3\left(\sqrt{\frac{1}{3}x + \frac{4}{3}}\right)^2 - 4 \\ &= 3\left(\frac{1}{3}x + \frac{4}{3}\right) - 4 \\ &= x + 4 - 4 \\ &= x \quad \checkmark \end{aligned}$$

Use the graph of f to find each value.

1) $f^{-1}(-3) = -6$

2) $f^{-1}(2) = -4.2$



HOMEWORK

p. 354-7: 1-12 (all),
36-44 (even),
45-56 (all),
72, 74

$$\textcircled{1} \quad f(x) = \begin{cases} 3x & \text{if } x < 0 \\ 2x-5 & \text{if } x \geq 0 \end{cases}$$

$$g(x) = \begin{cases} x+3 & \text{if } x \geq 1 \\ 5x & \text{if } x < 1 \end{cases} \quad g \circ f$$

$$\begin{array}{l} x < 0 \\ 0 \leq x < 1 \\ x \geq 1 \end{array} \quad g(x) = \begin{cases} 5x & x < 0 \\ 5x & 0 \leq x < 1 \\ x+3 & x \geq 1 \end{cases}$$

$$g(f(x)) = \begin{cases} 5(3x) & x < 0 \\ 5(2x-5) & 0 \leq x < 1 \\ 2x-5+3 & x \geq 1 \end{cases} \quad g \circ f = \begin{cases} 15x & x < 0 \\ 10x-25 & 0 \leq x < 1 \\ 2x-2 & x \geq 1 \end{cases}$$

$g \circ f$

$$\textcircled{2} \quad f(x) = \begin{cases} 2x & \text{if } x < 0 \\ 3x-5 & \text{if } x \geq 0 \end{cases} \quad g(x) = \begin{cases} x+4 & x \geq 1 \\ 4x & x < 1 \end{cases}$$

$$\begin{array}{l} x < 0 \\ 0 \leq x < 1 \\ x \geq 1 \end{array} \quad g(x) = \begin{cases} 4x & x < 0 \\ 4x & 0 \leq x < 1 \\ x+4 & x \geq 1 \end{cases}$$

$$g(f(x)) = \begin{cases} 4(2x) & x < 0 \\ 4(3x-5) & 0 \leq x < 1 \\ (3x-5)+4 & x \geq 1 \end{cases} = \begin{cases} 8x & x < 0 \\ 12x-20 & 0 \leq x < 1 \\ 3x-1 & x \geq 1 \end{cases}$$